**Class-incremental Novel Class Discovery (class-iNCD):**
Discovering novel categories in an unlabelled data set by leveraging a pre-trained model that has been trained on a labelled data set containing disjoint yet related categories, while preserving the ability of the model to recognize previously seen categories, without access to the previously seen data and task-id of an input sample during inference.

**Motivation**
- To facilitate learning of novel classes, we dedicate a task specific classifier that is optimized with robust rank statistics:
  \[ \ell_{novel} = -\mathbb{E}_{y_{nov}, y}(\log(p(y)) + (1 - \log(p(y)) \log(1 - p(y))) \]
- To overcome reliance on task-id, we propose to maintain a joint classifier for both the base and novel classes, which is trained with the pseudo-labels generated by the task specific one:
  \[ \ell_{self} = -\mathbb{E}_{y_{base}, y_{nov}, x}(\log(h_{base}(g(x))) \]
  \[ \hat{g}(x) = \mathcal{C}(x) + \text{arg max } \mathbb{E}_{y_{base}}(g(x)) \]
- We propose to store the base class feature prototypes from the previous task as exemplars. Features derived from the stored prototypes are then replayed to prevent forgetting old information on the base classes:
  \[ \ell_{replay} = -\mathbb{E}_{y_{base}, y_{nov}, x}(\log(h_{base}(g(x))) \]
- To keep the feature replay useful, we add a regularization on the current feature extractor:
  \[ \ell_{reg} = -\mathbb{E}_{y_{base}}[\|g(x) - \hat{g}(x)\|_2] \]
- We propose a novel framework, FRoST, that can tackle the newly introduced and relevant task of class-incremental novel class discovery (class-iNCD).
- Our FRoST is equipped with prototypes for feature-replay and employs feature-level knowledge distillation to prevent forgetting. Moreover, it uses pseudo-labels from the task specific head to efficiently learn novel classes without interference, enabling us to achieve a task-agnostic classifier.
- We run extensive experiments on three common benchmarks to prove the effectiveness of our method. FRoST also obtains state-of-the-art performance when compared with the existing baselines. Additionally, we run experiments on a sequence of tasks of unlabelled sets and verify its generality.

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**Overall Framework**
- **Task of Learning Old Classes**
  - Old Prototypes
  - Labeled data of old classes
  - After Training
  - \( L_{ce} \)
- **Task of Learning New Classes**
  - Net-old
  - Unlabelled data of new classes
  - Fixed
  - \( L_{mse} \)
  - \( L_{ce} \)

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